Boolean Properties of Sets — Requirements

Library Committee Association of Mizar Users

Summary. This article contains proofs of the theorems which are obvious if the directive 'requirements BOOLE;' will be added to environment declaration of the Mizar article.

MML Identifier: BOOLE.

WWW: http://mizar.org/JFM/Vol-3/boole.html

One can prove the following propositions:

- (1) For every set *X* holds $X \cup \emptyset = X$.
- (2) For every set *X* holds $X \cap \emptyset = \emptyset$.
- (3) For every set *X* holds $X \setminus \emptyset = X$.
- (4) For every set *X* holds $\emptyset \setminus X = \emptyset$.
- (5) For every set *X* holds $X \doteq \emptyset = X$.
- (6) For every set *X* such that *X* is empty holds $X = \emptyset$.
- (7) For all sets x, X such that $x \in X$ holds X is non empty.
- (8) For all sets *X*, *Y* such that *X* is empty and $X \neq Y$ holds *Y* is non empty.

Received April 30, 2002 Published January 2, 2004